

CLAIMS

1. Method of generating electronic keys d for a public-key cryptography method using an electronic device, mainly characterized in that it comprises two separate calculation steps:

Step A

1) calculating pairs of prime numbers (p,q) or values representative of pairs of prime numbers, this calculation being independent of knowledge of the pair (e,l) in which e is the public exponent and l is the length of the key of the cryptography method, l also being the length of the modulus N of said method,

2) storing the pairs or values thus obtained;

Step B

calculating a key d from the results of step A and knowledge of the pair (e,l) .

2. Method of generating electronic keys according to Claim 1, characterized in that step A-1) consists in calculating pairs of prime numbers (p,q) without knowledge of the public exponent e or of the length l of the key, using a parameter Π which is the product of small prime numbers, so that each pair (p,q) has a maximum probability of being able to correspond to a future pair (e,l) and can make it possible to calculate a key d .

3. Method of generating electronic keys according to Claim 2, characterized in that the calculation of step A-1) also takes account of the fact

that e has a high probability of forming part of the set $\{3, 17, \dots, 2^{16+1}\}$, and for this use is made in the calculation of a seed σ which makes it possible to calculate not pairs (p,q) but a representative value referred to as the image of the pairs (p,q) .

4. Method of generating electronic keys according to Claims 1 and 3, characterized in that the storage A-2) consists in storing the image of the pairs.

5. Method of generating electronic keys according to Claim 1, characterized in that step A-1) consists in calculating pairs of prime numbers (p,q) for different probable pairs (e,l) .

6. Method of generating electronic keys according to Claims 2 and 5, characterized in that the parameter Π contains the usual values of the public exponent e , for example 3, 17.

7. Method of generating electronic keys according to Claim 1, characterized in that step A-1) comprises an operation of compressing the calculated pairs (p,q) and step A-2) then consists in storing the compressed values thus obtained.

8. Method of generating electronic keys according to Claim 1, characterized in that step A-1) comprises the generation of a prime number q for which a lower limit B_0 is set for the length ℓ_0 of this prime number that is to be generated, such that $\ell_0 \geq B_0$, for example $B_0 = 256$ bits, and in that it comprises the following sub-steps:

1) calculating parameters v and w from the following relations and storing them:

$$v = \sqrt{2^{2\ell_0-1}}/\Pi$$

$$w = 2^{\ell_0}/\Pi$$

5 in which Π is stored and corresponds to the product of the f smallest prime numbers, f being selected such that $\Pi \leq 2^{B_0}$,

2) selecting a number j within the range of integers $\{v, \dots, w-1\}$ and calculating $\ell=j \Pi$;

10 3) selecting and storing a prime number k of short length compared to the length of an RSA key within the range of integers $\{0, \dots, \Pi-1\}$, (k, Π) being co-prime;

4) calculating $q=k+\ell$,

15 5) verifying that q is a prime number, if q is not a prime number then:

a) taking a new value for k using the following relation:

20 $k = a \cdot k \pmod{\Pi}$; a belonging to the multiplicative group Z^*_Π of integers modulo Π ;

b) repeating the method from step 4).

9. Method of generating electronic keys according to Claims 3 and 8, characterized in that the numbers j and k can be generated from the seed σ stored in memory.

10. Method of generating electronic keys according to Claim 8, characterized in that the prime number p is generated by repeating all the above sub-steps while replacing q with p and replacing ℓ_0 with $\ell - \ell_0$.

11. Method of generating electronic keys according to any one of the preceding claims, characterized in that:

5 step B comprises, for a pair (p,q) obtained in step A:

 - verifying the following conditions:

 (i) $p-1$ and $q-1$ are prime numbers with a given e and

10 (ii) $N=p*q$ is an integer of given length ℓ ,
 - if the pair (p,q) does not satisfy these conditions:

 - selecting another pair and repeating the verification until a pair is suitable,

15 - calculating the key d from the pair (p,q) obtained.

12. Secure portable object able to generate electronic keys d of an RSA-type cryptography algorithm, characterized in that it comprises at least:

20 - communication means for receiving at least one pair (e,l),

 - a memory for storing the results of a step A consisting in:

25 calculating pairs of prime numbers (p,q) or values representative of pairs of prime numbers, this calculation being independent of knowledge of the pair (e,l) in which e is the public exponent and l is the length of the key of the cryptography method, l also being the
30 length of the modulus N of this p ,

 - a program for implementing a step B consisting in:

 calculating a key d from the results of step A and knowledge of a pair (e,l).

13. Secure portable object according to Claim 12, characterized in that it also comprises a program for implementing step A, steps A and B being separate in terms of time.

14. Secure portable object according to Claim 13, characterized in that the program for implementing step A carries out the following sub-steps:

1) calculating parameters v and w from the following relations and storing them:

$$v = \sqrt{2^{2\ell_0-1}}/\Pi$$

$$w = 2^{\ell_0}/\Pi$$

in which Π is stored and corresponds to the product of the f smallest prime numbers, f being selected such that $\Pi \leq 2^{B_0}$, B_0 is a lower limit set for the length ℓ_0 of the prime number that is to be generated, such that $\ell_0 \geq B_0$, for example $B_0 = 256$ bits

2) selecting a number j within the range of integers $\{v, \dots, w-1\}$ and calculating $\ell = j \Pi$;

3) selecting and storing a prime number k of short length compared to the length of an RSA key within the range of integers $\{0, \dots, \Pi-1\}$, (k, Π) being co-prime;

4) calculating $q = k + \ell$,

5) verifying that q is a prime number, if q is not a prime number then:

a) taking a new value for k using the following relation:

$k = a \cdot k \pmod{\Pi}$; a belonging to the multiplicative group Z^*_Π of integers modulo Π ;

b) repeating the method from step 4).

15. Secure portable object according to Claim 12 or 13 or 14, characterized in that it consists of a chip card.